



Cambridge O Level

CANDIDATE
NAME

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CENTRE
NUMBER

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CANDIDATE
NUMBER

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ADDITIONAL MATHEMATICS

4037/21

Paper 2

May/June 2020

2 hours

You must answer on the question paper.

No additional materials are needed.

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Blank pages are indicated.

Mathematical Formulae**1. ALGEBRA***Quadratic Equation*

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a + b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n$$

where n is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series $u_n = a + (n-1)d$

$$S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a + (n-1)d\}$$

Geometric series $u_n = ar^{n-1}$

$$S_n = \frac{a(1-r^n)}{1-r} \quad (r \neq 1)$$

$$S_\infty = \frac{a}{1-r} \quad (|r| < 1)$$

2. TRIGONOMETRY*Identities*

$$\begin{aligned} \sin^2 A + \cos^2 A &= 1 \\ \sec^2 A &= 1 + \tan^2 A \\ \operatorname{cosec}^2 A &= 1 + \cot^2 A \end{aligned}$$

Formulae for $\triangle ABC$

$$\begin{aligned} \frac{a}{\sin A} &= \frac{b}{\sin B} = \frac{c}{\sin C} \\ a^2 &= b^2 + c^2 - 2bc \cos A \\ \Delta &= \frac{1}{2}bc \sin A \end{aligned}$$

- 1 Variables x and y are such that, when $\sqrt[4]{y}$ is plotted against $\frac{1}{x}$, a straight line graph passing through the points $(0.5, 9)$ and $(3, 34)$ is obtained. Find y as a function of x . [4]

- 2 (a) Write $9x^2 - 12x + 5$ in the form $p(x - q)^2 + r$, where p , q and r are constants. [3]

- (b) Hence write down the coordinates of the minimum point of the curve $y = 9x^2 - 12x + 5$. [1]

3 DO NOT USE A CALCULATOR IN THIS QUESTION.

$$p(x) = 15x^3 + 22x^2 - 15x + 2$$

(a) Find the remainder when $p(x)$ is divided by $x + 1$. [2]

(b) (i) Show that $x + 2$ is a factor of $p(x)$. [1]

(ii) Write $p(x)$ as a product of linear factors. [3]

- 4 (a) In an examination, candidates must select 2 questions from the 5 questions in section A and select 4 questions from the 8 questions in section B. Find the number of ways in which this can be done. [2]

- (b) The digits of the number 6378129 are to be arranged so that the resulting 7-digit number is even. Find the number of ways in which this can be done. [2]

- 5 The vectors \mathbf{a} and \mathbf{b} are such that $\mathbf{a} = \alpha\mathbf{i} + \mathbf{j}$ and $\mathbf{b} = 12\mathbf{i} + \beta\mathbf{j}$.

- (a) Find the value of each of the constants α and β such that $4\mathbf{a} - \mathbf{b} = (\alpha + 3)\mathbf{i} - 2\mathbf{j}$. [3]

- (b) Hence find the unit vector in the direction of $\mathbf{b} - 4\mathbf{a}$. [2]

- 6 Find the values of k for which the line $y = kx - 7$ and the curve $y = 3x^2 + 8x + 5$ do not intersect. [6]

7 (a) Solve the simultaneous equations

$$\begin{aligned}10^{x+2y} &= 5, \\10^{3x+4y} &= 50,\end{aligned}$$

giving x and y in exact simplified form.

[4]

(b) Solve $2x^{\frac{2}{3}} - x^{\frac{1}{3}} - 10 = 0$.

[3]

8 (a) Expand $(2-x)^5$, simplifying each coefficient.

[3]

(b) Hence solve $\frac{e^{(2-x)^5} \times e^{80x}}{e^{10x^4+32}} = e^{-x^5}$.

[4]

- 9 A particle travels in a straight line. As it passes through a fixed point O , the particle is travelling at a velocity of 3 ms^{-1} . The particle continues at this velocity for 60 seconds then decelerates at a constant rate for 15 seconds to a velocity of 1.6 ms^{-1} . The particle then decelerates again at a constant rate for 5 seconds to reach point A , where it stops.

(a) Sketch the velocity-time graph for this journey on the axes below.

[3]

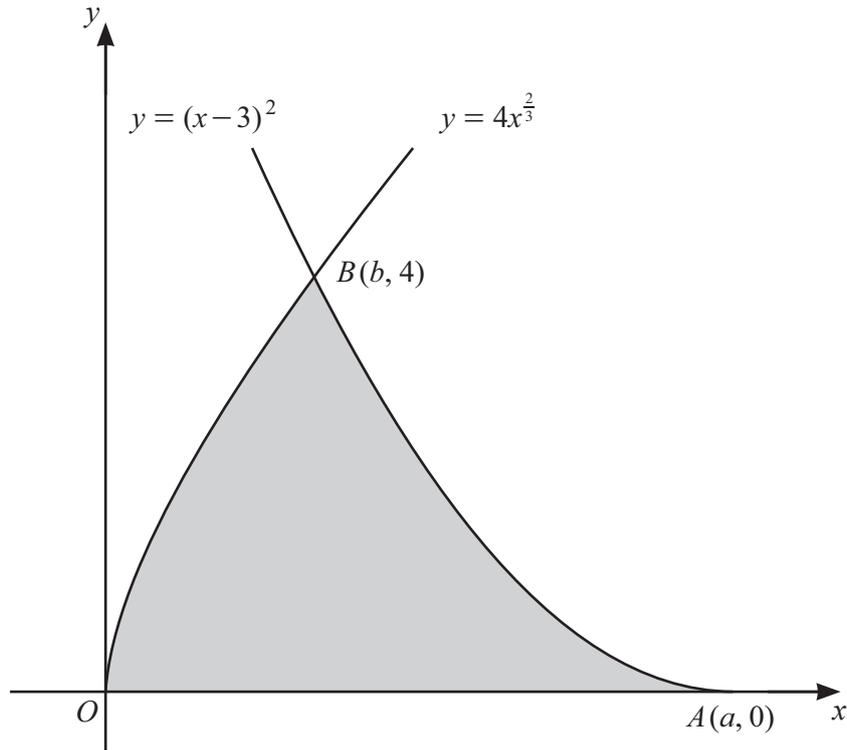


(b) Find the distance between O and A .

[3]

(c) Find the deceleration in the last 5 seconds.

[1]



The diagram shows part of the graphs of $y = 4x^{\frac{2}{3}}$ and $y = (x-3)^2$. The graph of $y = (x-3)^2$ meets the x -axis at the point $A(a, 0)$ and the two graphs intersect at the point $B(b, 4)$.

(a) Find the value of a and of b .

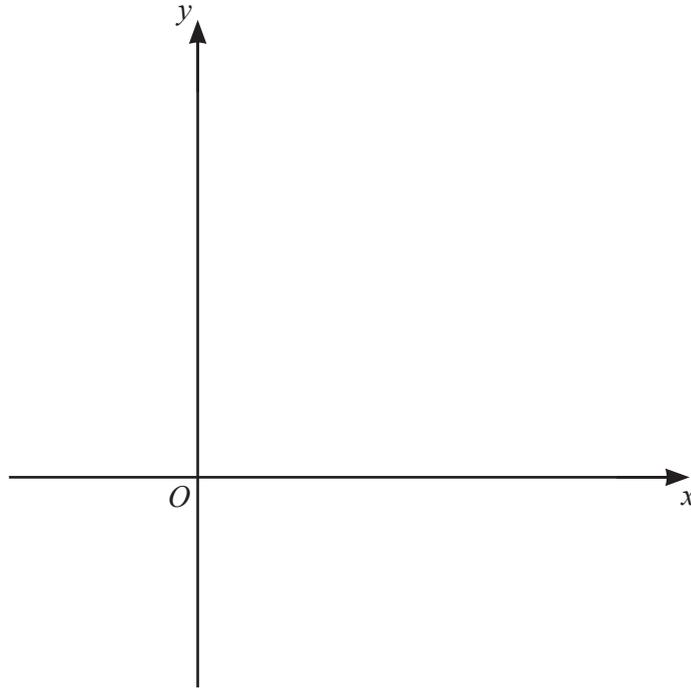
[2]

(b) Find the area of the shaded region.

[5]

11 The function f is defined by $f(x) = \ln(2x + 1)$ for $x \geq 0$.

(a) Sketch the graph of $y = f(x)$ and hence sketch the graph of $y = f^{-1}(x)$ on the axes below. [3]



The function g is defined by $g(x) = (x - 4)^2 + 1$ for $x \leq 4$.

(b) (i) Find an expression for $g^{-1}(x)$ and state its domain and range. [4]

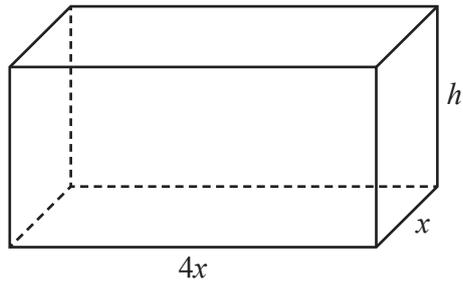
(ii) Find and simplify an expression for $fg(x)$. [2]

(iii) Explain why the function gf does not exist. [1]

12 (a) Find the x -coordinates of the stationary points of the curve $y = e^{3x}(2x+3)^6$. [6]

(b) A curve has equation $y = f(x)$ and has exactly two stationary points. Given that $f''(x) = 4x - 7$, $f'(0.5) = 0$ and $f'(3) = 0$, use the second derivative test to determine the nature of each of the stationary points of this curve. [2]

(c) In this question all lengths are in centimetres.



The diagram shows a solid cuboid with height h and a rectangular base measuring $4x$ by x . The volume of the cuboid is 40 cm^3 . Given that x and h can vary and that the surface area of the cuboid has a minimum value, find this value. [5]

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